

Formal Modelling and Analysis of a Self-Adaptive Robotic System

or On Modelling and Analysing Autonomous Underwater Robots as Probabilistic Featured Transition Systems

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joint work with **Juliane Päßler**, Einar Broch Johnsen, S. Lizeth Tapia Tarifa (U Oslo)
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1 November 2024

REMARO
RELIABLE AI FOR MARINE ROBOTICS



Publications

- **Formal Modelling and Analysis of a Self-Adaptive Robotic System (iFM'23)**
 - Model: SAS from underwater robotics domain as *probabilistic FTS* with *dynamic feature switching*
 - Analysis: reward and safety properties with the *feature-aware probabilistic model checker ProFeat*
- **A Configurable Software Model of a Self-Adaptive Robotic System (SCP'25)**
 - Artefact published as *original software publication*
- **Analysing Self-Adaptive Systems as Software Product Lines (JSS'25?)**
 - Natural correspondence between SAS (*external self-adaptation* and *managed + managing* sub-system) and DSPL (*150% SPL family model* with a controller switching features during runtime)
 - Further adaptation: additional sensors with varying priorities, possible need to abort a mission
- **Feature-Oriented Modelling and Analysis of a Self-Adaptive Robotic System (FAC'25?)**
 - Further analyses using not only **PRISM** as backend but also **Storm** for *parametric model checking* and *multi-objective queries* (achievability, numerical, Pareto) depending on analysed properties:
 - Safety guarantees concerning mission duration and energy usage
 - Impact of different environments on the safety guarantees
 - Parameter synthesis to analyse the effect of environmental conditions
 - Trade-offs between mission duration and energy usage
 - ...

<https://pchrson.github.io/profeat>

<https://www.prismmodelchecker.org/>

<https://www.stormchecker.org/>



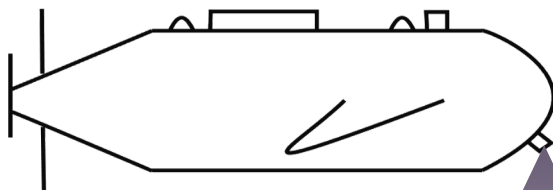
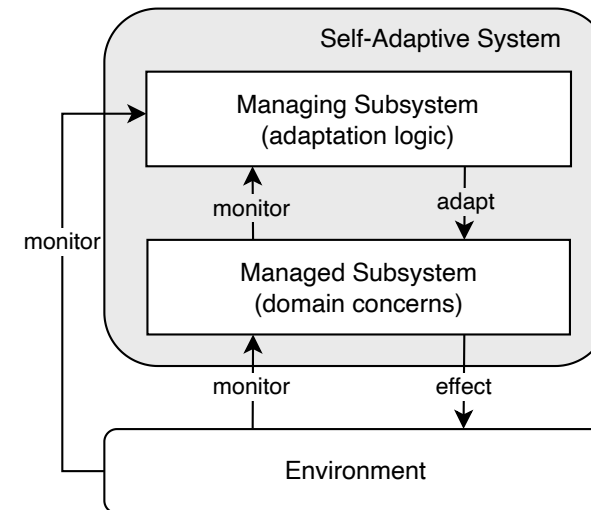
Analyse Self-Adaptive Systems as Dynamic Software Product Lines with ProFeat

P. Chrszon, C. Dubslaff, S. Klüppelholz, C. Baier,
**ProFeat: Feature-Oriented Engineering for
Family-Based Probabilistic Model Checking.**
Formal Aspects of Computing 30 (2018), 45–75.

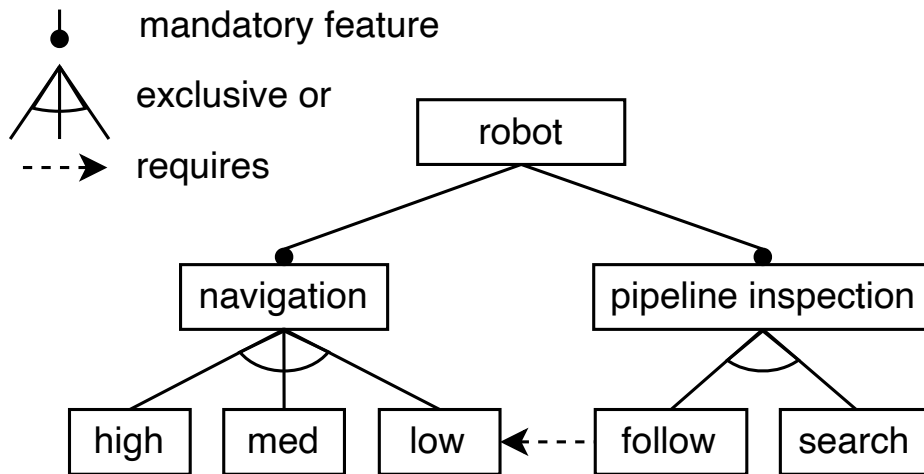
Family-based model checking provides a means to *simultaneously* model check, in a *single* run, properties of a *family* of models, each representing a different *configuration*

Pipeline Inspection

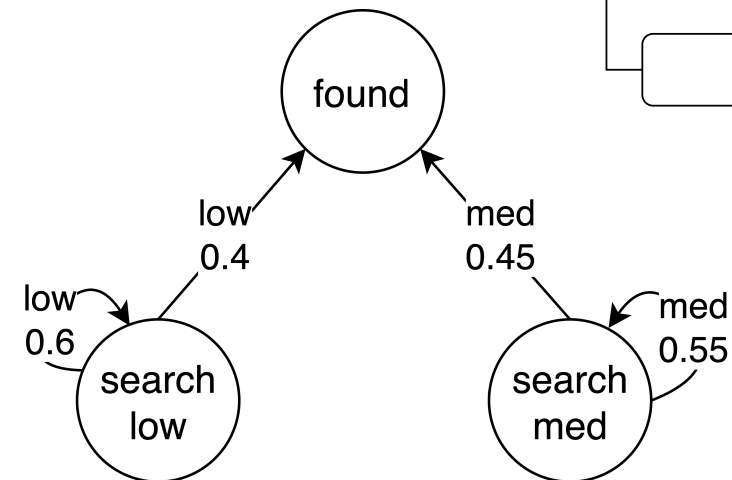
G. Rezende Silva, J. Päßler, J. Zwanepol, E. Alberts, S.L. Tapia Tarifa, Gerostathopoulos, E.B. Johnsen & C. Hernández Corbato, **SUAVE: An Exemplar for Self-Adaptive Underwater Vehicles**. *Proceedings of the 18th International Symposium on Software Engineering for Adaptive and Self-Managing Systems (SEAMS 2023)*, IEEE, 2023.



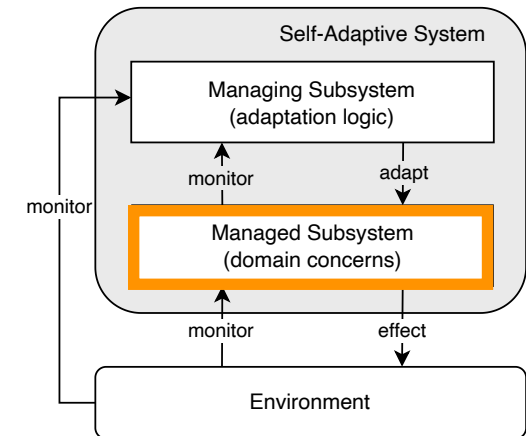
Probabilistic Featured Transition System



Feature Model

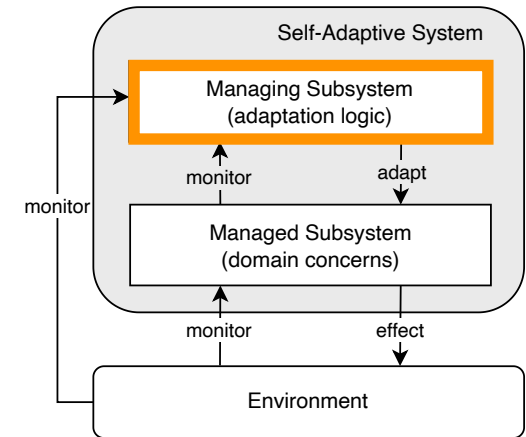
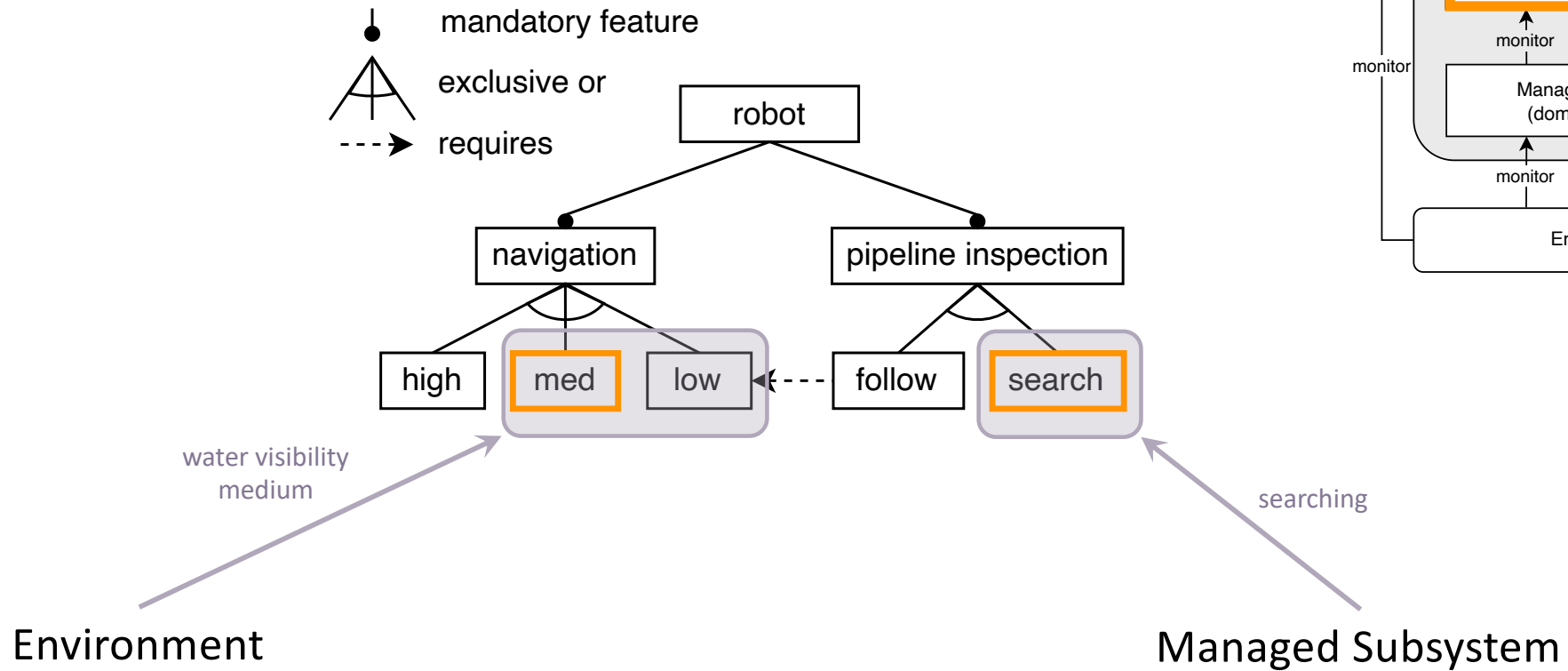


Probabilistic FTS

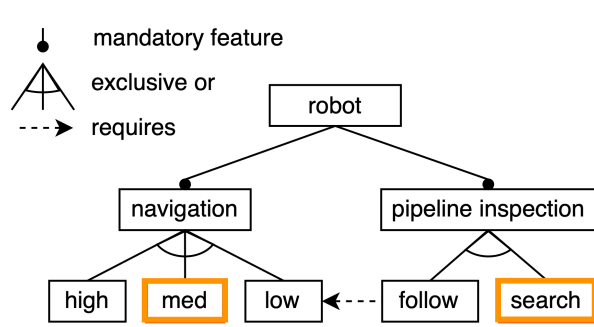


A. Classen, M. Cordy, P.-Y. Schobbens, P. Heymans, A. Legay, J.-F. Raskin, **FTS: Foundations for Verifying Variability-Intensive Systems and Their Application to LTL Model Checking**. *IEEE Transactions on Software Engineering* 39 (2013)

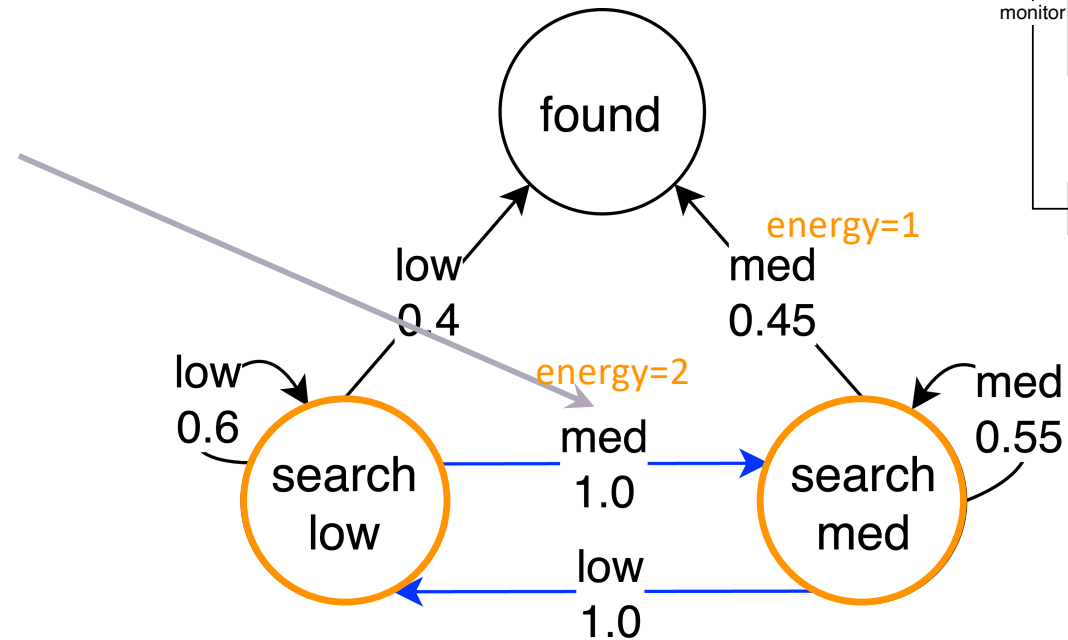
Managing Subsystem



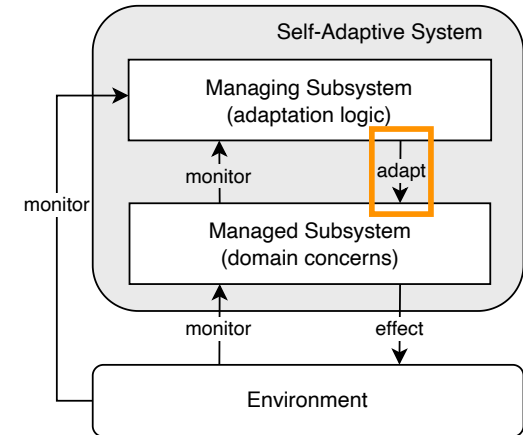
Adaptation



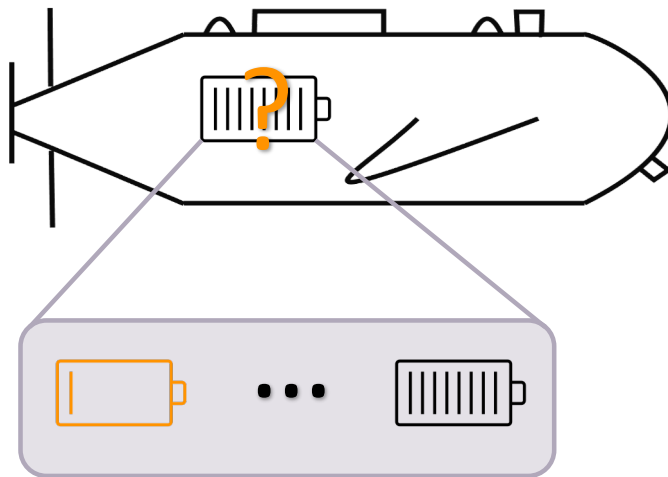
Managing Subsystem



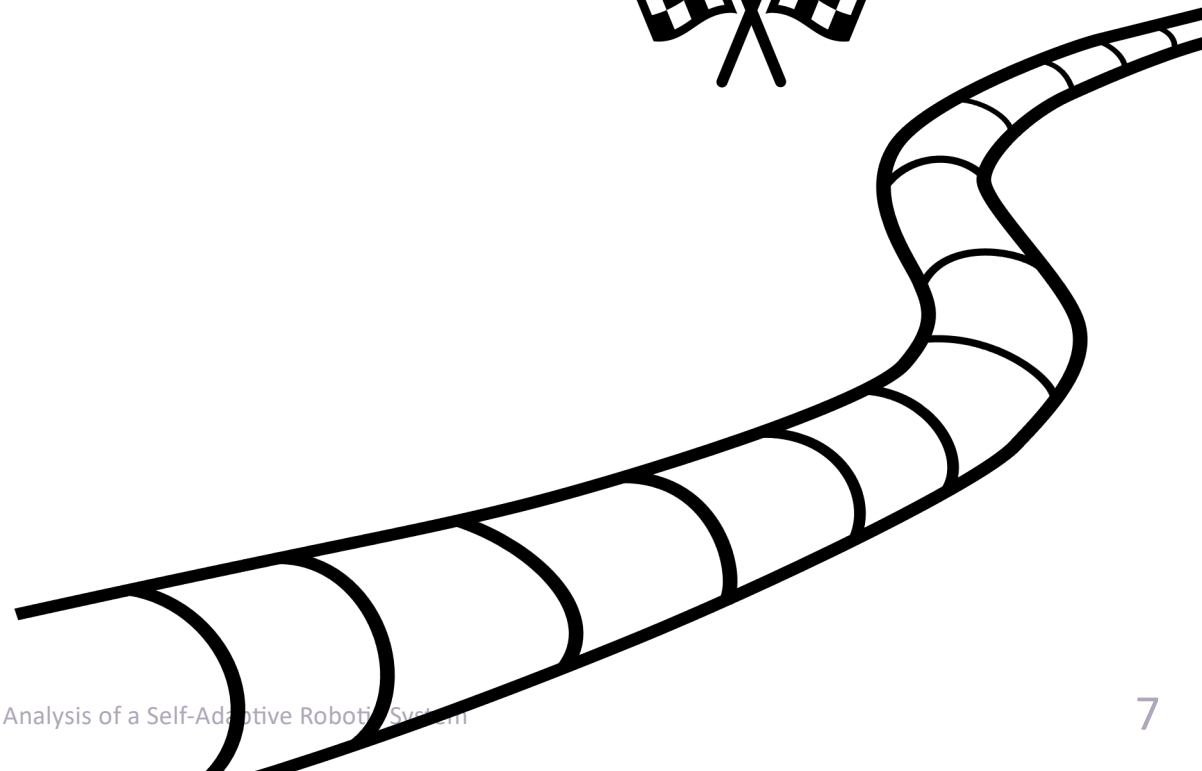
Managed Subsystem



Costs/Rewards



Probabilities

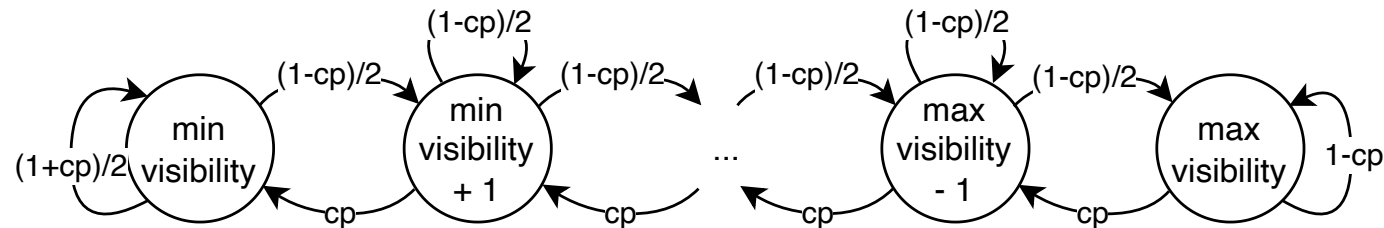


Costs/Rewards

```
1 root feature
2   all of robot;
3   modules auv, environment;
4   rewards "time"
5     [step] true : 1;
6   endrewards
7   rewards "energy"
8     // Costs for being in a recovery state
9     (s=recover_high) : 2;
10    // .. omitted code ..
11
12    // Costs for switching altitudes
13    (s=search_high) & active(low) : 4;
14    (s=search_high) & active(med) : 2;
15    (s=found) & active(high) : 4;
16    (s=found) & active(med) : 2;
17    // .. omitted code ..
18  endrewards
19 endfeature
```

Probabilities

```
1 module auv
2   s : [0..12] init start_task;
3   d_insp : [0..inspect] init 0;
4   t_failed : [0..infl_tf] init 0;
5
6   // .. omitted code ..
7   // From search state to another state
8   [step] (s=search_high & active(high)) -> 0.59:(s'=found)
9     + 0.4:(s'=search_high) + 0.01:(s'=recover_high);
10  [step] (s=search_high & active(med)) -> 1:(s'=search_med);
11  [step] (s=search_high & active(low)) -> 1:(s'=search_low);
12  // .. omitted code ..
13
14  // Following the pipeline
15  [step] (s=following) & (d_insp<inspect) & (t_failed=0)
16    -> 0.9: (s'=following) & (d_insp'=d_insp+1)
17    + 0.07: (s'=lost_pipe) + 0.03:(s'=recover_following)
18    & (t_failed'=(t_failed<infl_tf? t_failed+1 : t_failed));
19  // .. omitted code ..
20  [step] (s=following) & (d_insp=inspect) -> (s'=done);
21
22  // Lost the pipeline
23  [step] (s=lost_pipe) -> 1: (s'=start_task) & (t_failed'=0);
24  // .. omitted code ..
25 endmodule
```



```
1 module environment
2   water_visib : [min_visib..max_visib]
3     init round((max_visib-min_visib)/2);
4   [step] true -> current_prob: (water_visib'= (water_visib=min_visib?
5     min_visib:water_visib-1)) + (1-current_prob)/2: (water_visib'=
6     (water_visib=max_visib? max_visib:water_visib+1))
7     + (1-current_prob)/2: true;
8 endmodule
```

```
1 formula med_visib = (max_visib-min_visib)/3;
2 formula high_visib = 2*(max_visib-min_visib)/3;
3
4 controller
5   // Change altitude depending on water visibility
6   [step] (s!=found) & active(search) & water_visib < med_visib
7     -> activate(low) & deactivate(high) & deactivate(med);
8   [step] (s!=found) & active(search)
9     & med_visib <= water_visib & water_visib < high_visib
10    -> activate(low) & deactivate(med) & deactivate(high);
11  [step] (s!=found) & active(search)
12    & med_visib <= water_visib & water_visib < high_visib
13    -> activate(med) & deactivate(low) & deactivate(high);
14  // .. omitted code ..
15
16  // Switch task from "search" to "follow"
17  [step] (s=found) & active(search)
18    -> deactivate(search) & activate(follow) & activate(low)
19        & deactivate(med) & deactivate(high);
20
21  // Switch task from "follow" to "search"
22  [step] (s=lost_pipe) & active(follow)
23    -> deactivate(follow) & activate(search);
24
25  // Enable transitions when following the pipeline
26  [step] (s!=lost_pipe) & active(follow) -> true;
27 endcontroller
```

ProFeat Analysis: Energy and Duration

Scenario	min_visib	max_visib	current_prob	inspect
1 (North Sea)	1	10	0.6	10
2 (Caribbean Sea)	3	20	0.3	30

- 1 `R{"energy"}min=? [F ${s=done}]`;
- 2 `R{"energy"}max=? [F ${s=done}]`;

Scenario	Energy		Time	
	min	max	min	max
1	24.78	44.39	23.66	32.40
2	59.08	4723.29	55.54	1315.58

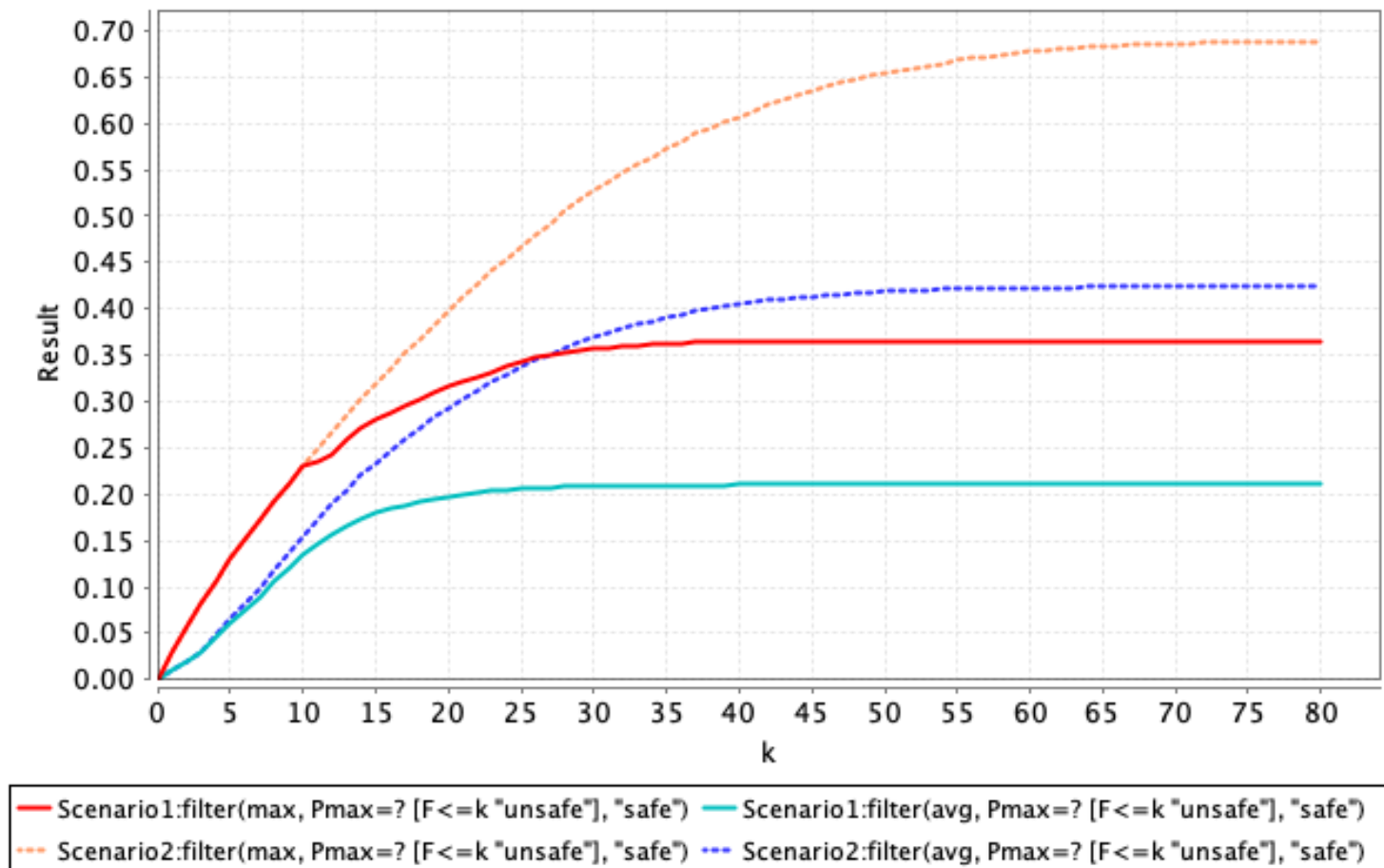
ProFeat Analysis: Unsafe States

```
1 label "unsafe" = s=recover_high | s=recover_med | s=recover_low
2               | s=recover_following;
3 label "safe" = s=start_task | s=lost_pipe | s=start_search | s=search_high
4              | s=search_med | s=search_low | s=found | s=following | s=done;
5 Pmin=? [G "safe"];
6 filter(min, Pmin=? [ F<=k "safe" ], "unsafe");
7 filter(max, Pmax=? [ F<=k "unsafe" ], "safe");
8 filter(avg, Pmax=? [ F<=k "unsafe" ], "safe");
```

The minimum probability of only taking safe states (cf. Line 6) was shown to be 0.65 for Scenario 1 and 0.32 for Scenario 2.

In both of the scenarios, the probability of reaching a safe state from an unsafe state (cf. line 7) is above 0.95 after 5 time steps and above 0.99 after 7 time steps.

ProFeat Analysis: Unsafe States



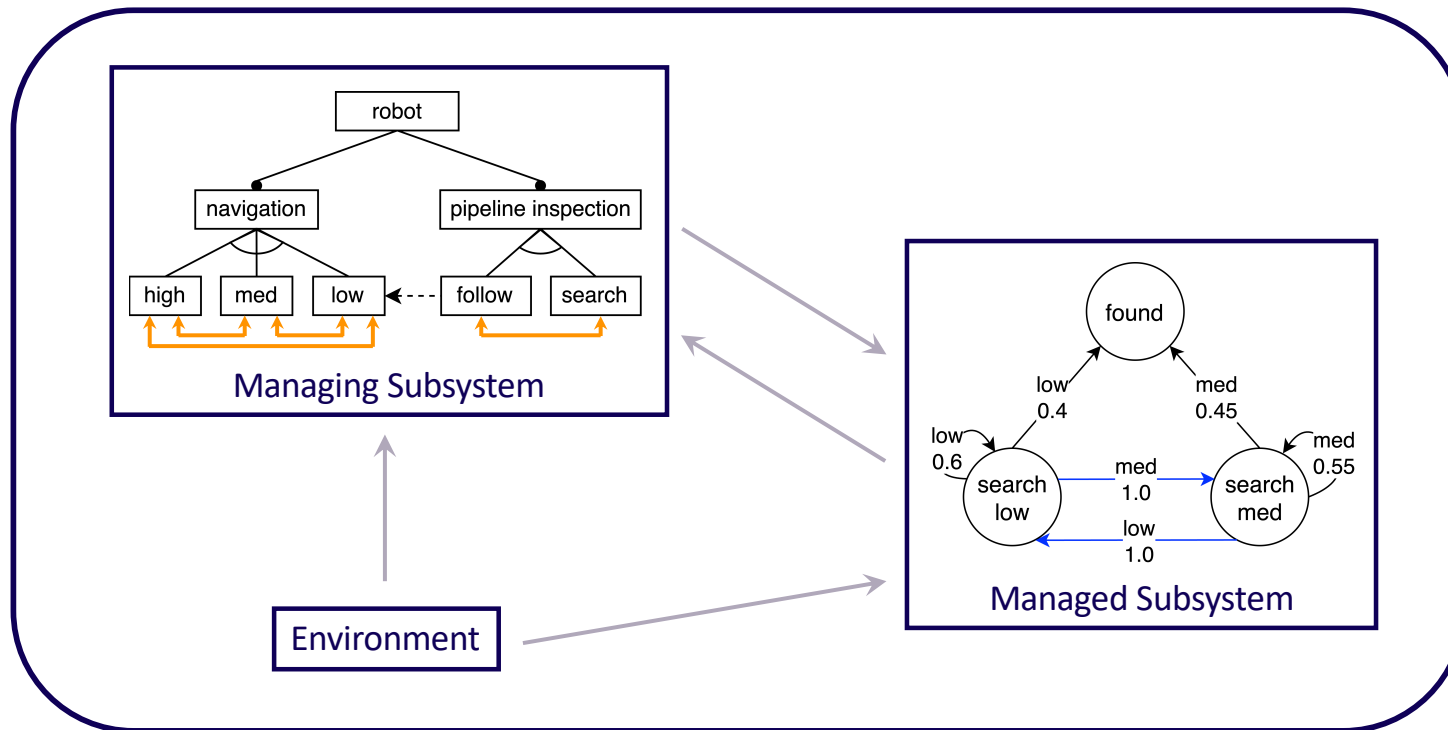
Context

- *External self-adaptation*: separation of concerns between the application logic (the managed subsystem) and the adaptation logic (the managing subsystem) of the SAS
 - *Bounded adaptivity* by modelling context variation that is anticipated at design time
 - Dynamic SPLs have been proposed before to manage runtime reconfiguration for self-adaptive robots, yet it is still considered an **unsolved challenge**: *“there is a need to validate the proposals, either in an industrial environment or in different test cases, expanding the application areas”*
- O. Aguayo and S. Sepúlveda, **Variability management in dynamic software product lines for self-adaptive systems—A systematic mapping**. *Applied Sciences* 12 (2022)
- K. Yoshimura, chief researcher at Hitachi, in his keynote address *“The 20-year journey of SPLE in Hitachi and the next”* during SPLC’23, presented the use of dynamic SPLs for autonomous robotic systems as a **new industrial challenge**

https://2023.splc.net/wp-content/uploads/2023/09/SPLC2023_Keynotes-1.pdf

Summary

Analyse SASs as DSPLs: ProFeat with family-based analysis



iFM'23 paper



SCP'25 paper

