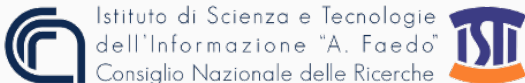


# Efficient Static Analysis and Family-based Model Checking of SPL Models

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Maurice ter Beek



joint work with Ferruccio Damiani, Luca Paolini, Giordano Scarso (University of Turin, IT), Michael Lienhardt (ONERA, FR) and Franco Mazzanti (FMT, ISTI-CNR, Pisa, IT)

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SES'23, Tokyo, Japan, August 25<sup>th</sup>, 2023

- Member of FMT lab at ISTI–CNR since '03, lab head since '19
- MSc ('96) and PhD ('03) degrees from Leiden University (NL)
- Positions in HU ('95-'96,'02), BE ('05), IT ('00-'01), NL ('12-'13,'15)



# Why am I here?

General co-chair, with Paolo Arcaini, of **SPLC 2023** (NII, next week)

Local chair: Fuyuki Ishikawa (NII)



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David Benavides (U Seville, SP) Data-intensive PLs: Embracing past results and new variability challenges

Hideto Ogawa & Kentaro Yoshimura (Hitachi Ltd, JP) The 20-year journey of SPLE in Hitachi and the next

Marianne Huchard (U Montpellier, FR) Chronicles of concept lattices: Unveiling structure in the software world

- Behavioural variability modelling and analysis of SPL models
  - Product- vs. family-based analysis
  - Featured Transition System (FTS)
  - Ambiguities: dead/false optional transitions, hidden deadlocks
- Automated static analysis of FTSs
  - Detecting ambiguities: criteria, SAT solving, implementation
  - Disambiguating FTSs: example and benchmark experiments
- Modal Transition System with variability constraints ( $MTS_v$ )
- VMC: family-based model checking of  $MTS_v$ s
- FTS4VMC: family-based model checking of  $MTS_v$ s *and* FTSs
- Conclusions and Future Work

# Background

---

# Software Product Lines (SPLs)

- Configurable (software) system whose variants (products) differ by the provided **features**, i.e. the functionality that is relevant for an end-user

# Product lines are everywhere

Configure your BMW vehicle


http://www.bmw.com/en/general/carconfigurator/content.html

BMW dealer Brochures Corporate/Direct Sales Shop BMW Financial Services Used Vehicles

Home 1 2 3 4 5 6 7 X Z4 BMW M BMW i BMW Owners BMW Insights

Configure vehicle

The International BMW website



BMW  
Driving Pleasure

## Configure your BMW vehicle

Are you interested in configuring your ideal BMW? Please select a country to visit the configurator in the Virtual Center or contact your local BMW dealer who will be happy to answer all your questions about the BMW model you are interested in.

## Related topics



Request information  
Order product catalogues,  
brochures and equipment  
lists direct from BMW.

## FIND YOUR BMW.



### Filter

> Reset filter

Budget

Vehicle type

All

Petrol

Diesel

Hybrid

Electric Vehicle

Body type

Saloon

Touring

Convertible

Coupé

Gran Turismo

Sports Hatch

Roadster

Sports Activity Coupé

Sports Activity Vehicle

Number of seats

30 Vehicles **465 Model variants**



**BMW 1 Series 3-door Sports Hatch (34)**  
from £ 17,775.00



**BMW 1 Series 5-door Sports Hatch (39)**  
from £ 18,305.00



**BMW 2 Series Coupé (14)**  
from £ 24,265.00



**BMW 3 Series Saloon (56)**  
from £ 23,550.00



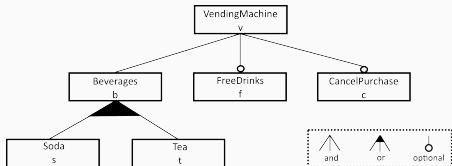
**BMW 3 Series Touring (54)**  
from £ 24,865.00



**BMW 3 Series Gran Turismo (39)**  
from £ 29,200.00

# Feature models

- Configurable (software) system whose variants (products) differ by the provided features, i.e. the functionality that is relevant for an end-user



**Feature Model** (diagram) of a beverage vending machine

# Feature models analysis

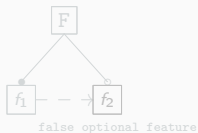
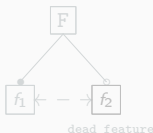
- Configurable (software) system whose variants (products) differ by the provided features, i.e. the functionality that is relevant for an end-user



Benavides *et al.*, Automated Analysis of Feature Models 20 Years Later: a Literature Review. *Inf. Syst.*, 2010

# SPL analysis

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Benavides et al., Automated Analysis of Feature Models 20 Years Later: a Literature Review. *Inf. Syst.*, 2010

- Popular in embedded / critical systems domain: formal modelling and analysis techniques to prove SPL **behaviour** correct are widely studied  
Thüm et al., A classification and survey of analysis strategies for SPLs. *ACM Comput. Surv.*, 2014
- Challenge known formal methods & tools by potentially high number of different variants, each giving rise to a large state space, in general

# Scalability is an issue

(examples by C. Kästner, CMU, Pittsburgh, USA)

33 optional, independent  
features



a unique configuration/variant for every

person on this planet

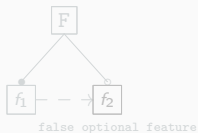
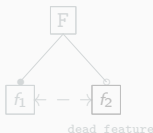
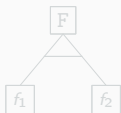
320<sup>optional, independent</sup> features

more configurations/variants than estimated

atoms in the universe

# SPL analysis

- Configurable (software) system whose variants (products) differ by the provided features, i.e. the functionality that is relevant for an end-user



Benavides et al., Automated Analysis of Feature Models 20 Years Later: a Literature Review. *Inf. Syst.*, 2010

- Popular in embedded / critical systems domain: formal modelling and analysis techniques to prove SPL behaviour correct are widely studied  
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  - Challenge known formal methods & tools by potentially high number of different variants, each giving rise to a large state space, in general
- ⇒ Lift success stories known for single systems (products) to sets of products (families) by exploiting **variability** modelling and analysis

## Product- vs. family-based analysis

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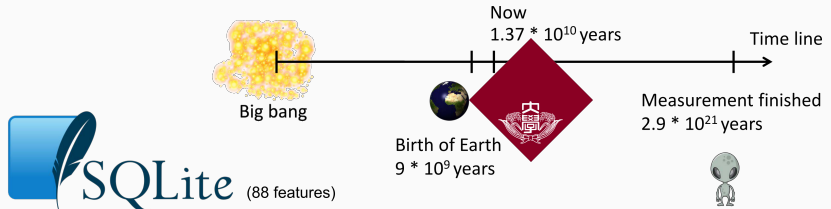
## Product-based analysis:

- 👍 Simple, brute-force approach
- 👍 Make use of standardly available, highly optimised analysis tools

# Product-based analysis: inefficient, if not infeasible

(example by S. Apel, Saarland University, Germany)

- 👍 Simple, brute-force approach
- 👍 Make use of standardly available, highly optimised analysis tools
- 👎 Number of product variants is exponential in number of features
- 👎 Same piece of behaviour or code is verified numerous times, as many times as the number of variants that are able to execute it








## Solution: family-based analysis

- 👍 Beneficial in case of many products with substantial similarities
- 👍 Same piece of behaviour (or code) is verified only once, regardless of how many variants can produce it

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-  Requires (compact) family models (superimposed, *150% models*)
  
-  Dedicated **variability-based** models, logics, and model checkers (e.g. FTS, MTS $v$ , Feature Net, PL-CCS, fLTL, fCTL,  $v$ -ACTL, QFLan, SNIP, VMC)


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Dimovski et al., Family-based model checking without a family-based model checker @ SPIN'15

Chrszon et al., Family-based modeling and analysis for probabilistic systems: featuring ProFeat @ FASE'16

ter Beek et al., Family-Based Model Checking with mCRL2 @ FASE'17

Dimovski et al., Variability-specific Abstraction Refinement for Family-based Model Checking @ FASE'17

Dimovski, Abstract Family-Based Model Checking Using Modal Featured Transition Systems @ FASE'18

ter Beek et al., Family-Based SPL Model Checking Using Parity Games with Variability @ FASE'20

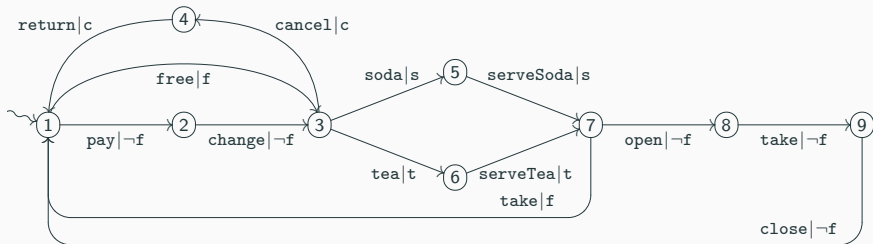
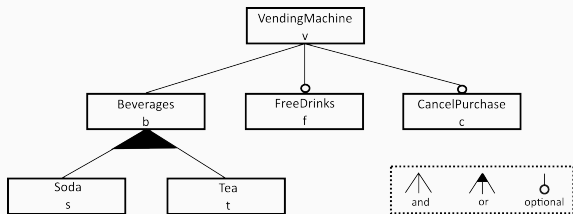
# Featured Transition Systems (FTSs)

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# From LTS to FTS

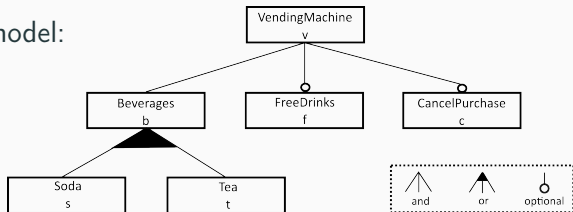
An FTS adds to an LTS a feature model and so-called **feature expressions**

Classen *et al.*, Model checking lots of systems @ ICSE'10 (MIP Award @ SPLC'20), FTSs. *IEEE TSE*, 2013



# FTS of example SPL: a vending machine

Feature model:

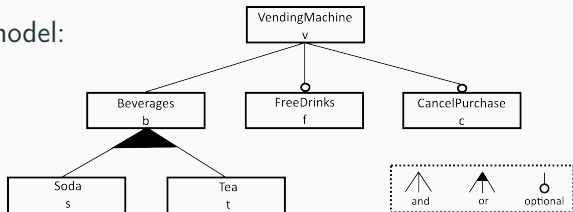


12 valid products

e.g.,  $\{v, b, s, t\}$ ,  $\{v, b, s, c\}$

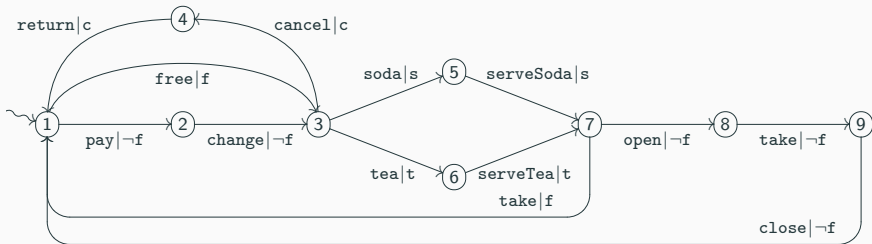
# FTS of example SPL: a vending machine

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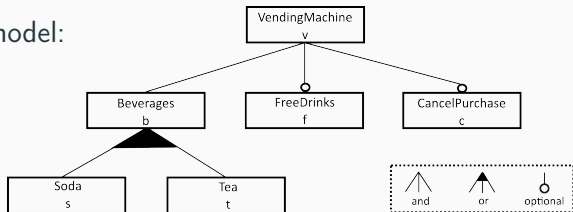
FTS of 12 valid products (LTSs)

e.g., {v,b,s,t}, {v,b,s,c}



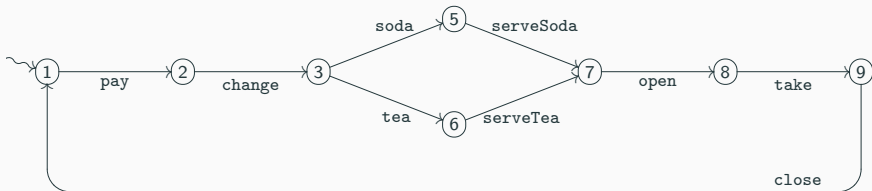
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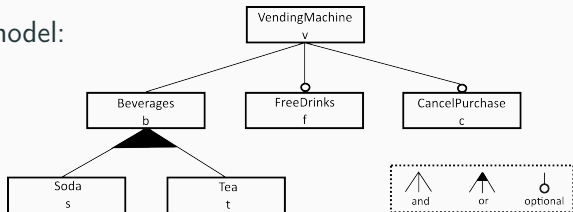
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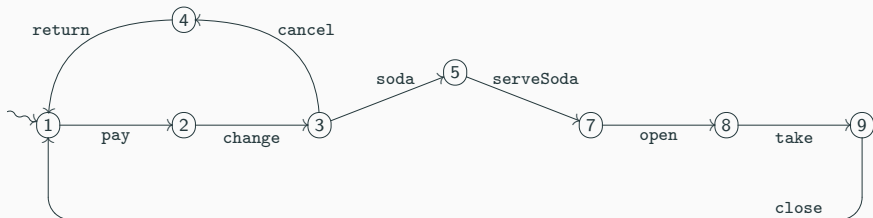
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# Ambiguities in behavioural SPL models

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## Key idea and aim of our SPLC'19 paper



Mimick anomaly detection known from feature model analysis in behavioural SPL models (FTSs) by automated static analysis:

1. dead transitions
2. false optional transitions
3. hidden deadlock states

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Mimick anomaly detection known from feature model analysis in behavioural SPL models (FTSs) by automated static analysis:

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2. false optional transitions
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Catch and offer means to remove possible ambiguities in FTSs:

1. Ambiguous FTSs are undesired: provide unclear ideas of the SPLs
2. Unambiguous FTSs pave way to efficient family-based verification

**dead transition**

an FTS transition not reachable in any product (LTS)

## dead transition

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**false optional transition** a featured FTS transition which is

1. not dead
2. not annotated with feature expression  $\top$  (true, i.e., selected)
3. present in every FTS product in which its source state is present

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## hidden deadlock state an FTS state which is

1. not a deadlock (i.e., it has outgoing transitions) in the FTS
2. a deadlock (i.e., no outgoing transitions) in some FTS product

---

*Deadlock freedom* is an important safety property: a system should not reach a state where no further action is possible, thus guaranteeing *progress* or *liveness*; for configurable systems, this extends to guaranteeing liveness for all system variants (products)

## Ambiguous FTS $\rightarrow$ unambiguous FTS [skip]

### Transformation:

1. remove dead transitions

## Ambiguous FTS $\rightarrow$ unambiguous FTS [skip]

### Transformation:

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2. turn false optional transitions into *must* transitions (i.e., labelled with  $\top$ )

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Step (3) must be performed only for the hidden deadlock states that have not yet become explicit deadlock states upon the removal of dead transitions in step (1)

## Ambiguous FTS $\rightarrow$ unambiguous FTS [skip]

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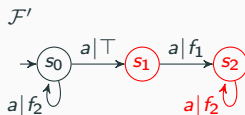
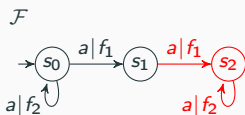
1. remove dead transitions
2. turn false optional transitions into *must* transitions (i.e., labelled with  $\top$ )
3. make hidden deadlock states  $s$  explicit:
  - 3.1 add a deadlock state  $s_{\dagger} \notin S$
  - 3.2  $\forall s$ : add a *deadlock transition* from  $s$  to  $s_{\dagger}$  labelled with  $\dagger \notin \Sigma$  and with a feature expression that negates the disjunction of the feature expressions of all outgoing transitions of  $s$

---

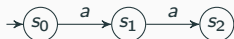
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# Example transformations [skip]

Feature Model:  $f_1 \oplus f_2$



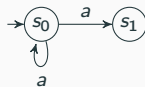
$\mathcal{F}|_{\lambda_1} = \mathcal{F}'|_{\lambda_1}$



$\mathcal{F}|_{\lambda_2}$



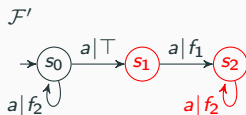
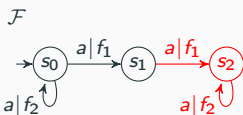
$\mathcal{F}'|_{\lambda_2}$



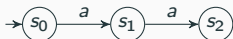
products  $\lambda_1 = \{f_1\}$  and  $\lambda_2 = \{f_2\}$

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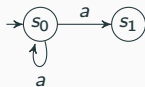
$$\mathcal{F}|_{\lambda_1} = \mathcal{F}'|_{\lambda_1}$$



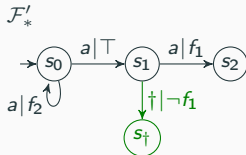
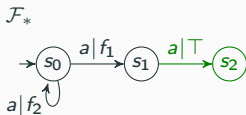
$$\mathcal{F}|_{\lambda_2}$$



$$\mathcal{F}'|_{\lambda_2}$$



products  $\lambda_1 = \{f_1\}$  and  $\lambda_2 = \{f_2\}$



# Efficient static analysis of FTSs

---

## One-by-one vs. all-in-one [recall]

Recall: family-based (all-in-one) analysis

- The analysis of ambiguities for a **single SPL's product** is an expensive (feasible) task that can be automatised
- To apply the “brute force” by analysing **all products of an SPL** is too expensive to be used in concrete cases
- However products of an SPL share a common “piece of code”, thus analysing each product individually (brute-force analysis) would involve a lot of **redundancy**

How to leverage this commonality and analyse the whole product line at once, bringing the total analysis time down, is a our goal !

## Implementation in Z3

FTS ambiguity detection problem is NP-complete: we used a SAT tool!

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FTS ambiguity detection problem is **NP-complete**: we used a SAT tool!

- We implemented our algorithm in Z3
- We made our implementation publicly available, including all benchmark examples used in the rest of the talk
- Our artefact received the ACM reusable badge:



[SPLC'19]

# Implementation in Z3

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[SPLC'19]

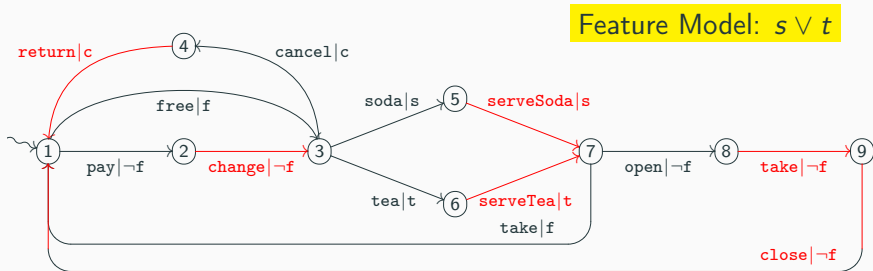
Z3 is a cross-platform Satisfiability Modulo Theories (SMT) solver (that includes a SAT solver) developed by Microsoft:

- it is freely available under the MIT license
- it supports arithmetic, fixed-size bit-vectors, extensional arrays, datatypes, uninterpreted functions, and quantifiers
- its typical applications are static checking, test-case generation, and predicate abstraction

# Example and benchmark experiments

---

# Example static analysis: vending machine



## Result of static analysis on FTS

Vending Machine: live

LIVE STATES = [1,2,3,4,5,6,7,8,9]

DEAD TRANSITIONS = []

FALSE OPTIONAL TRANSITIONS = [(2,3),(4,1),(5,7),(6,7),(8,9),(9,1)]

HIDDEN DEADLOCK STATES = []

# Benchmark experiments (1/3) [EMSE22]

FTS	characteristics			results of static analysis				computational effort	
	S	$ \delta $	$ \Sigma $	live-ness	# dead transitions	# false optional transitions	# hidden deadlock states	run-time (s)	memory usage (Mb)
Vending machine <small>Classen, PhD thesis, 2011</small>	9	13	12	yes	0	6	0	0.26	29.765
Coffee machine <small>Asirelli et al. @ SPLC'11</small>	14	23	15	yes	0	14	0	0.29	30.305
Soup component <small>Belder et al. @ FMSPL'15</small>	13	28	18	yes	0	7	0	0.316	30.85
Mine pump (system) <small>Classen, PhD thesis, 2011</small>	25	41	22	no	0	25	1	0.344	31.704
Mine pump (controller) <small>Classen, PhD thesis, 2011</small>	77	104	22	no	0	59	4	0.548	36.295
Coffee/Soup machine <small>Belder et al. @ FMSPL'15</small>	182	691	33	yes	8	284	0	37.766	119.427
Mine pump (complete) <small>Classen, PhD thesis, 2011</small>	418	1,255	26	yes	0	308	0	98.994	119.127
Claroline <small>Devroey et al. @ VaMoS'14</small>	107	11,236	106	yes	0	259	0	2413.8	2010.229

The experiments were performed on a virtual machine Gentoo 201905, CLI Version VirtualBox (VDI) 64 bit, with 2048 Mb of allocated memory on a Windows 10 Pro 64 bit with 16 Gb of RAM and CPU AMD Ryzen 7 1700X (8 core, 16 threads, 3.4 Ghz)

# Benchmark experiments (2/3) [SPLC19] vs. [EMSE22]

FTS	characteristics			computational effort				results
				implementation [SPLC19]		implementation [EMSE22]		runtime speedup
	S	$ \delta $	$ \Sigma $	runtime (s)	memory usage (Mb)	runtime (s)	memory usage (Mb)	
Vending machine <small>Classen, PhD thesis, 2011</small>	9	13	12	0.92	38.230	0.26	29.765	3.54x
Coffee machine <small>Asirelli et al. @ SPLC'11</small>	14	23	15	2.822	40.140	0.29	30.305	9.72x
Soup component <small>Belder et al. @ FMSPL'15</small>	13	28	18	2.544	40.870	0.316	30.85	8.05x
Mine pump (system) <small>Classen, PhD thesis, 2011</small>	25	41	22	2.192	41.899	0.344	31.704	6.37x
Mine pump (controller) <small>Classen, PhD thesis, 2011</small>	77	104	22	8.12	49.091	0.548	36.295	14.82x
Coffee/Soup machine <small>Belder et al. @ FMSPL'15</small>	182	691	33	timeout	–	37.766	119.427	>7200.00x
Mine pump (complete) <small>Classen, PhD thesis, 2011</small>	418	1,255	26	timeout	–	98.994	119.127	>7200.00x
Claroline <small>Devroey et al. @ VaMoS'14</small>	107	11,236	106	timeout	–	2413.8	2010.229	>7200.00x

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# Benchmark experiments (3/3) [liveness only]

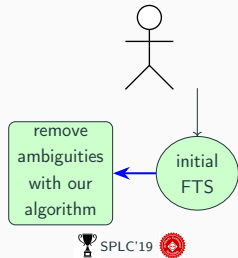
FTS	characteristics			computational effort				results
				full-fledged implementation		specialised implementation		
Model	$ S $	$ \delta $	$ \Sigma $	runtime (s)	memory usage (Mb)	runtime (s)	memory usage (Mb)	runtime fraction
Coffee/Soup machine <small>Belder et al. @ FMSPL'15</small>	182	691	33	37.766	119.427	2.288	61.620	6.06%
Mine pump (complete) <small>Classen, PhD thesis, 2011</small>	417	1,255	26	98.994	119.127	2.948	68.969	2.97%
Claroline <small>Devroey et al. @ VaMoS'14</small>	107	11,236	106	2413.8	2010.229	86.752	551.888	3.59%

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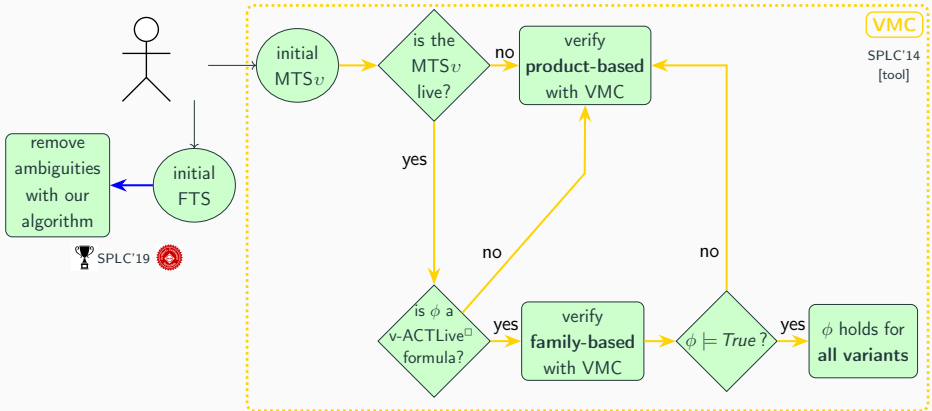
**Wrap up so far and outlook for tooling**

---

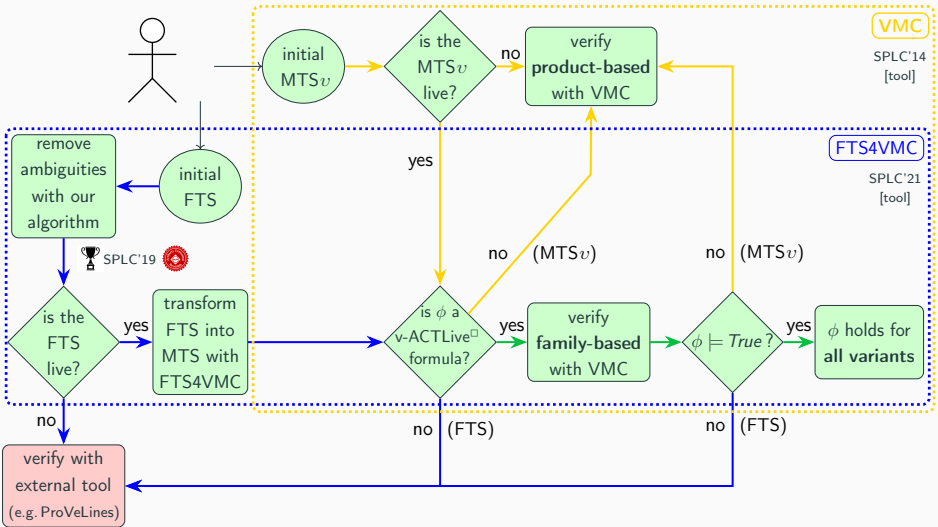
# Detect and remove ambiguities



# VMC: model checking MTS<sub>v</sub>



# FTS4VMC: front-end for VMC: model checking $MTS_v$ /FTS



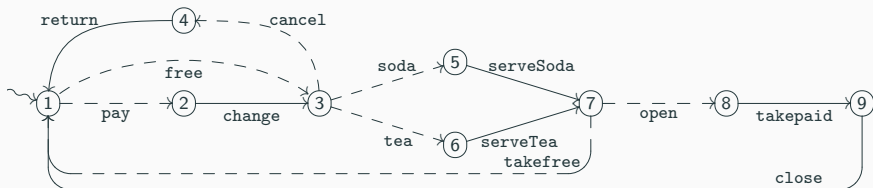
# Modal Transition Systems (MTSs) with variability constraints (MTS $v$ )

---

# MTS<sub>v</sub> of example SPL

An MTS<sub>v</sub> adds to an LTS so-called **may** and **must** transitions  
+ (variability) constraints

Asirelli *et al.*, Formal Description of Variability in Product Families @ SPLC'11  
ter Beek *et al.*, Modelling and analysing variability in product families. *JLAMP*, 2016

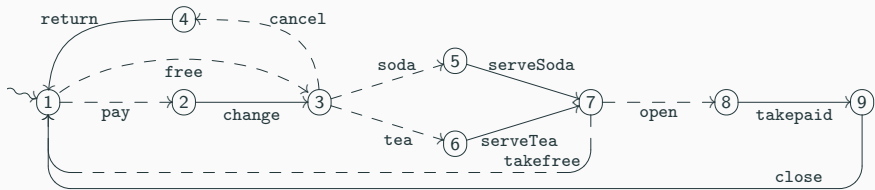


Constraints {

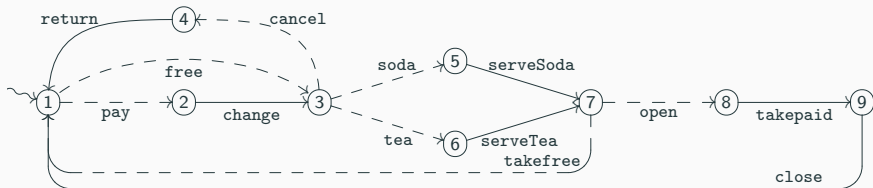
```
pay ALT free      // precisely one must be present
soda OR tea      // at least one must be present
takefree IFF free // either both or none are present
open ALT takefree // precisely one must be present
```

}

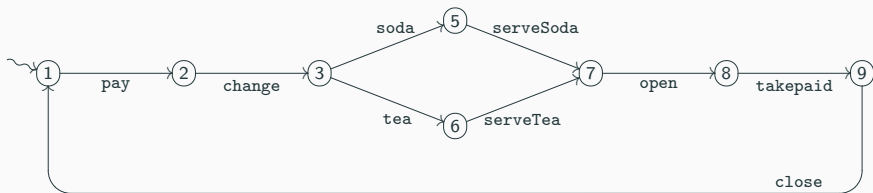
# Product LTSs of $MTS_v$ of example SPL



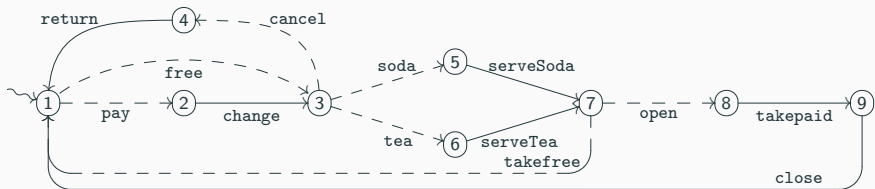
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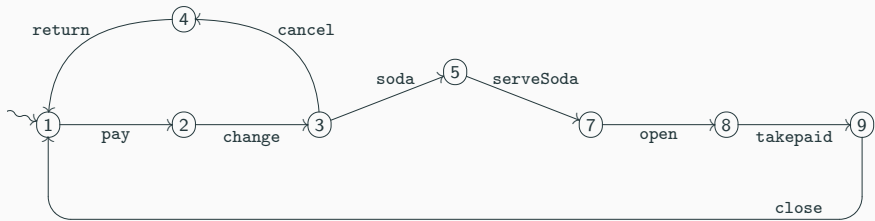
⇓ {pay,soda,tea,open}



# Product LTSs of $MTS_v$ of example SPL



⇓ {pay, cancel, soda, open}



# VMC: family-based model checking MTSs

---

# Variability analysis strategies supported by VMC

ter Beek & Mazzanti, VMC @ FM'12, SPLC'14

VMC:

- Input models in the form of a set of process-algebraic definitions
- Displays all possible family evolutions in the form of an MTS graph
- Supports a comprehensive temporal logic interpreted on  $L^2TSs$

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VMC offers product- and family-based model checking of MTS *vs*:

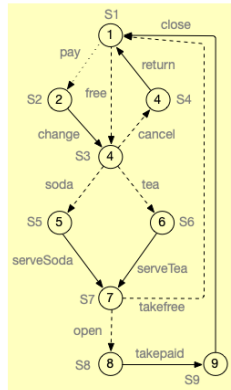
- Allows to verify (some of the) properties such that they hold for **all** LTS products of the MTS family ... and to receive feedback when such properties do not hold ('family-based')
- Allows to generate all valid products of an MTS family ... and to separately verify properties on them (product-based)

... with a **linear complexity**

# VMC input: textual model encoding as process definitions



```
1
2 -- VENDING MACHINE - MTSv version
3
4 S1 = pay(may) .S2
5     + free(may) .S3
6 S2 = change(must) .S3
7 S3 = cancel(may) .S4
8     + soda(may) .S5
9     + tea(may) .S6
10 S4 = return(must) .S1
11 S5 = serveSoda(must) .S7
12 S6 = serveTea(must) .S7
13 S7 = takefree(may) .S1
14     + open(may) .S8
15 S8 = takepaid(must) .S9
16 S9 = close(must) .S1
17
18
19 net SYS = S1
20
21 Constraints {
22   pay ALT free
23   soda OR tea
24   takefree IFF free
25   open ALT takefree
26 }
27
28
29
30
31
```



## Vending Machine: family-based model checking with VMC

The properties preserved for all LTS products are those that hold for **all** possible executions—and use a **live** fragment of the  $MTS_v$  (**live implies no hidden deadlocks!**)

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VMC notifies whenever preservation of an analysis result applies:

The screenshot displays the VMC V6.5 (2019) interface. On the left is a green sidebar with navigation buttons: Edit Model, View Current Model, Explore the MTS, Draw Family MTS, Generate Products, Welcome, and Quit. Below these is a small image of a bridge labeled 'Kandinsky 1908'. The main window shows the following text:

**The Formula:**  $AF \{serveSoda \text{ or } (serveTea \text{ or } cancel)\} \text{ true}$   
is **TRUE**

The formula holds for ALL the MTS variants  
(evaluation time= 0.062 sec.)

---

(total states generated= 8, computations fragments generated= 12, total evaluation time= 0.062 sec.)

At the bottom, the formula  $AF \{serveSoda \text{ or } serveTea \text{ or } cancel\}$  is shown next to a button labeled 'Check The Formula Explain the Result'.

# Vending Machine: product-based model checking with VMC

VMC lists for each product the action labels of all may transitions that have been preserved (as must transitions) in that product LTS

VMC V6.5  
(2019)

● ● ● ● ●

New Model ...

Edit Current Model

Explore the MTS


View Current Model

Draw Family MTS

Generate Products

Welcome

Quit



Kandinsky 1908

Evaluation of the formula "[pay] AF {takePaid} true" on all family products

<a href="#">product+CancelPurchase+FreeDrinks+Soda+Tea_12</a>	Formula evaluates	TRUE
<a href="#">product+CancelPurchase+FreeDrinks+Soda_08</a>	Formula evaluates	TRUE
<a href="#">product+CancelPurchase+FreeDrinks+Tea_10</a>	Formula evaluates	TRUE
<a href="#">product+CancelPurchase+FreeDrinks+Tea_10</a>	Formula evaluates	TRUE
<a href="#">product+CancelPurchase+Soda+Tea_06</a>	Formula evaluates	FALSE
<a href="#">product+CancelPurchase+Soda_02</a>	Formula evaluates	FALSE
<a href="#">product+CancelPurchase+Tea_04</a>	Formula evaluates	FALSE
<a href="#">product+FreeDrinks+Soda+Tea_11</a>	Formula evaluates	TRUE
<a href="#">product+FreeDrinks+Soda_07</a>	Formula evaluates	TRUE
<a href="#">product+FreeDrinks+Tea_09</a>	Formula evaluates	TRUE
<a href="#">product+Soda+Tea_05</a>	Formula evaluates	TRUE
<a href="#">product+Soda_01</a>	Formula evaluates	TRUE
<a href="#">product+Tea_03</a>	Formula evaluates	TRUE

Logic Formula for all Products

[pay] AF {takePaid} true

Check The Formula	Explain the Result
-------------------	--------------------

**FTS4VMC: front-end for VMC (family-based model checking FTSs and FTSs)**

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## Family-based model checking: v-ACTLive<sup>□</sup>

v-ACTLive<sup>□</sup>: fragment of Action-based CTL with dedicated  
**variability-aware** versions of temporal operators

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Note

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(must  $\rightarrow$  necessary transitions, featured  $\rightarrow$  optional transitions,  
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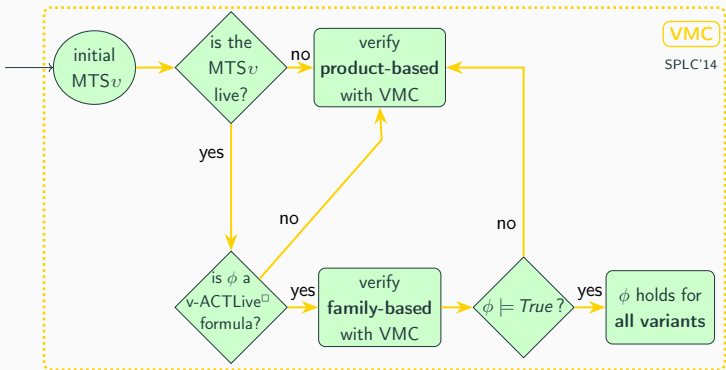
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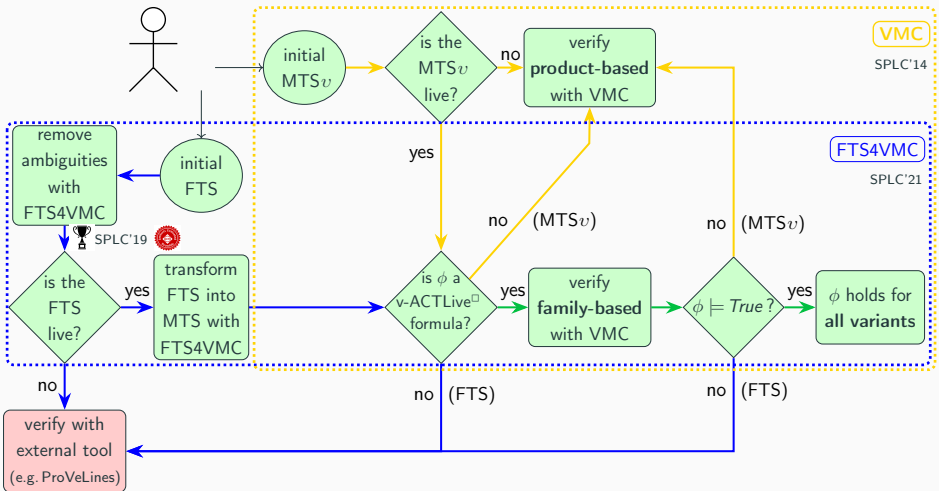
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# Toolchain: family-based model checking of MTS<sub>v</sub>s



# Toolchain: family-based model checking of $MTS_v$ s *and* FTSs



The **green** blocks are automated by the toolchain (FTS4VMC+VMC)

The **blue** and **green** steps (applied to FTSs) are realised by FTS4VMC

## Conclusions and Future Work

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4. Ongoing work:
  - integrating FTS2PROMELA transformation

## References

- SPLC19 M.H. ter Beek, F. Damiani, M. Lienhardt, F. Mazzanti, and L. Paolini, Static Analysis of Featured Transition Systems. In Proceedings 23rd International Systems and Software Product Line Conference (SPLC'19), ACM, 2019, 39–51 (**best paper**) <https://doi.org/10.1145/3336294.3336295>
- EMSE22 M.H. ter Beek, F. Damiani, M. Lienhardt, F. Mazzanti, and L. Paolini, Efficient Static Analysis and Verification of Featured Transition Systems. *Empirical Software Engineering* 22, 1 (2022), 10:1–10:43 <https://doi.org/10.1007/s10664-020-09930-8>
- SPLC21 M.H. ter Beek, F. Mazzanti, F. Damiani, L. Paolini, G. Scarso, M. Valfrè, and M. Lienhardt, Static Analysis and Family-based Model Checking of Featured Transition Systems with VMC. In Proceedings 25th International Systems and Software Product Line Conference (SPLC'21), ACM, 2021 (**tool demo**) <https://doi.org/10.1145/3461002.3473071>
- SCP22 M.H. ter Beek, F. Damiani, M. Lienhardt, F. Mazzanti, L. Paolini, and Giordano Scarso, FTS4VMC: A front-end tool for static analysis and family-based model checking of FTSs with VMC. *Science of Computer Programming* 224 (2022), 102879 (**original software publication**) <https://doi.org/10.1016/j.scico.2022.102879>

## Family-based model checking (1/2): $v$ -ACTLive<sup>□</sup> [recall]

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Thus:

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## Family-based model checking with SPIN . . .

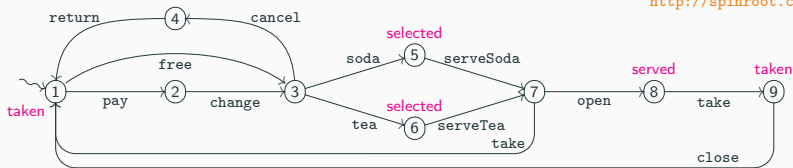
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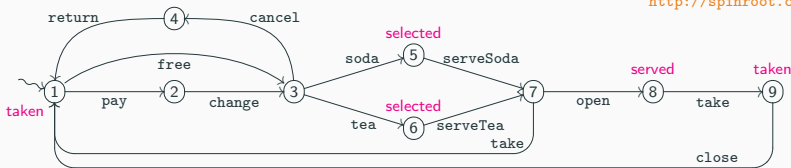
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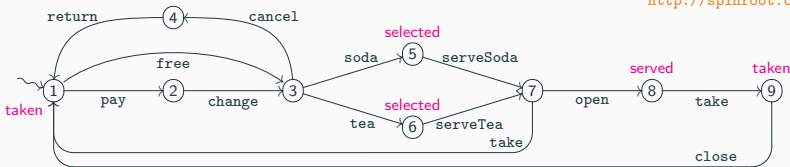


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