

# Quantitative Variability Modeling and Analysis

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## ABSTRACT

The explicit management of variability in the development cycle of software-intensive systems has led to a plethora of modeling and analysis techniques tailored to deal with behavioral validation of such configurable systems. Most of the work, however, focuses on qualitative (i.e. functional) requirements. Recently, there is growing interest in variability modeling and analysis techniques that do explicitly consider quantitative (i.e. non-functional) requirements, such as dependability, energy consumption, security, and cost.

Today's software is embedded in a variety of smart and critical systems that run in environments where events occur randomly and affect the system, and to which it needs to adapt. Therefore, quantitative modeling and analysis is currently a hot topic. The panel on Quantitative Variability Modeling and Analysis (QSPL) discusses the latest quantitative techniques and how to apply them to variability modeling and analysis of software-intensive systems.

## CCS CONCEPTS

• **Software and its engineering** → **Formal methods; Extra-functional properties; Software product lines.**

## KEYWORDS

Variability, Quantitative modeling, Quantitative analysis, QSPL

### ACM Reference Format:

Maurice H. ter Beek and Axel Legay. 2019. Quantitative Variability Modeling and Analysis. In *13th International Workshop on Variability Modelling of Software-Intensive Systems (VaMoS '19)*, February 6–8, 2019, Leuven, Belgium. ACM, New York, NY, USA, 2 pages. <https://doi.org/10.1145/3302333.3302349>

## 1 BACKGROUND AND MOTIVATION

Software Product Line Engineering (SPLE) concerns engineering, in a *cost-effective* and *time-efficient* manner, *configurable* software-intensive systems. The key issue is to manage *variability* among the products (or variants) of a Software Product Line (SPL), typically expressed in terms of *features*. Products share a set of core features, but differ with respect to product-specific features, meaning that a product can be seen as a set of features. A set of products (or family) is defined by a *feature model*.

The explicit management of variability in software development causes complexity in SPL *modeling and analysis*. An important example concerns *behavioral validation*, i.e., guaranteeing that each product of the family satisfies a series of behavioral requirements. Variants of this problem include computing a set of products that

do not satisfy the requirements together with a justification. A common approach to assess such requirements consists of building the system and testing it. However, if the system should fail to meet the requirements, then costly interactions are needed to improve it. This problem is amplified in SPLE, where the number of products typically grows exponentially with the number of features. In fact, it is generally acknowledged that two major challenges with respect to behavioral validation of SPLs are i) to offer a compact and efficient way of modeling the behavior of families of products, and ii) to offer efficient analysis algorithms to exploit such models [44].

Throughout this decade, we witnessed numerous efforts on lifting well-known formal specification languages and formal verification techniques from (single system) software engineering to SPLE (or configurable systems), cf., e.g., [4–6, 9, 12, 19, 21–24, 29, 32, 45, 46] and the more exhaustive references in [7, 51]. However, the vast majority of work on variability modeling and analysis focuses on *qualitative* (i.e., functional) requirements. Only recently, we are witnessing a growing interest in variability modeling and analysis techniques that explicitly consider *quantitative* (i.e., non-functional) requirements, like dependability, which encompasses attributes like availability and reliability, but also energy consumption, security, and cost [8, 10, 11, 16, 17, 26–28, 30, 31, 35, 36, 39, 43, 47, 49].

Today's software is embedded in a wide variety of *smart* and *critical* systems (e.g., aircraft, railways, automotive, and medical devices) that run in environments where events occur *randomly* and affect the system (e.g., think of failures) and to which it needs to *adapt*. For these reasons, quantitative modeling and analysis (e.g., through probabilistic systems and probabilistic or statistical model checking) is nowadays receiving a lot of attention. In the specific setting of configurable software-intensive systems, this requires modeling and analysis techniques able to cope with the complexity of systems stemming from behavior, variability, and randomness.

In [7], we coined the term *Quantitative Variability Modeling and Analysis* (QSPL) with the aim to cover the following kind of topics:

- Quantitative specification and verification techniques for systems with variability;
- Modeling and analysis of real-time, hybrid or probabilistic systems with variability;
- Analysis of safety, security or dependability properties of systems with variability;
- Modeling and analysis of dynamic, adaptive and (runtime) reconfigurable systems.

Many open questions remain regarding the gap between research on verification and that on variability, in particular involving quantities. Hence, the time is ripe for a QSPL panel to address issues such as:

- How to relate quantities with variability?
- How to incorporate quantities in (textual) languages for variability modeling? (cf. [1, 18, 42])
- How do quantities influence the (space-time) trade-off between product-based and family-based analyses (cf. [47]) and can (qualitative) abstractions be of help? (cf. [3, 13, 25])
- How about the robustness and sensitivity of quantitative variability modeling and analysis? (cf. [15, 37])

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VAMOS '19, February 6–8, 2019, Leuven, Belgium  
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ACM ISBN 978-1-4503-6648-9/19/02.  
<https://doi.org/10.1145/3302333.3302349>

## 2 PANELISTS

The following gender-balanced set of panelists, most of whom never participated at VaMoS before, guarantees interesting discussions with our community on how to handle quantitative notions in SPLE.

Christel Baier (TU Dresden, Germany) is an expert in probabilistic model checking and quantitative analysis of stochastic systems and she has recently started applying this to SPLs [16, 17, 30, 31, 40].

Maxime Cordy (U Luxembourg) is an expert on behavioral modeling and analysis of SPLs, in particular based on featured transition systems, with affinity to quantitative approaches [19–21, 24–28, 49].

Uli Fahrenberg (École polytechnique, France) is an expert in quantitative extensions of transition systems, in particular weighted transition systems, and quantitative logics, including recent applications to behavioral SPL models [2, 14, 34–36, 47].

Mariëlle Stoelinga (U Twente, Netherlands) is an expert on quantitative modeling and analysis, in particular based on probabilistic, stochastic or timed automata models, and quantitative logics, but she has not yet been active in SPLE [33, 38, 41, 48, 50].

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